

p. 84 #69-72, 73-84 ($\frac{1}{2}$ but do #82)

HW

p. 69 #6, 10, 18, 21-24, 31, 32, 37, 80, 81

Do these

① Without a calc., draw a graph, list transformations,
write using function notation

(a) $f(x) = 3(x+4)^2 - 1$

(b) $f(x) = -\frac{1}{2}|x-1| + 2$

$h(x) = 3f(x+4) - 1$

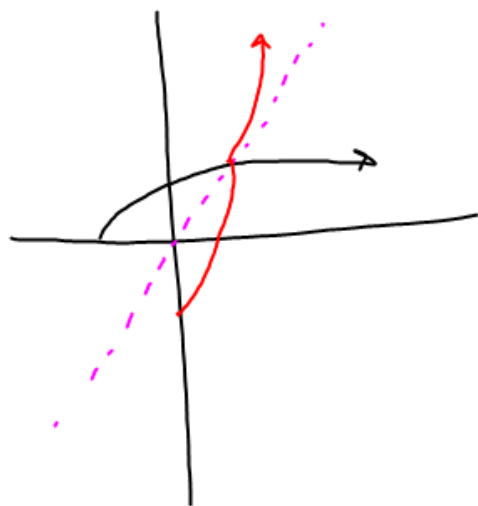
$h(x) = -\frac{1}{2}f(x-1) + 2$

vert stretch
left
down
up
flip x-axis
vert. compression
right

② Find the inverses of each

(c) $f(x) = 4x + 9$

$y = \frac{x-9}{4}$



(d) $f(x) = \frac{\sqrt{x+2}}{5}$

$y = \frac{\sqrt{x+2}}{5}$

$5 \cdot x = \frac{\sqrt{y+2}}{5} \cdot 5$

$(5x)^2 = (\sqrt{y+2})^2$

$25x^2 = y + 2$

$25x^2 - 2 = y$

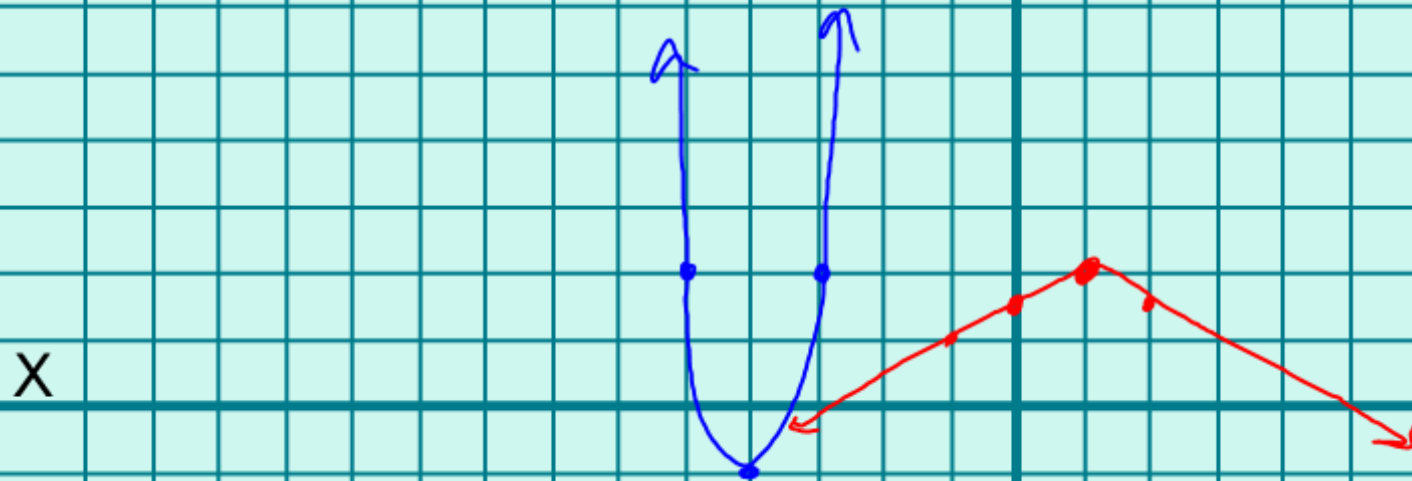
① replace $f(x)$ w/ y

* ② Switch x & y

③ solve for y

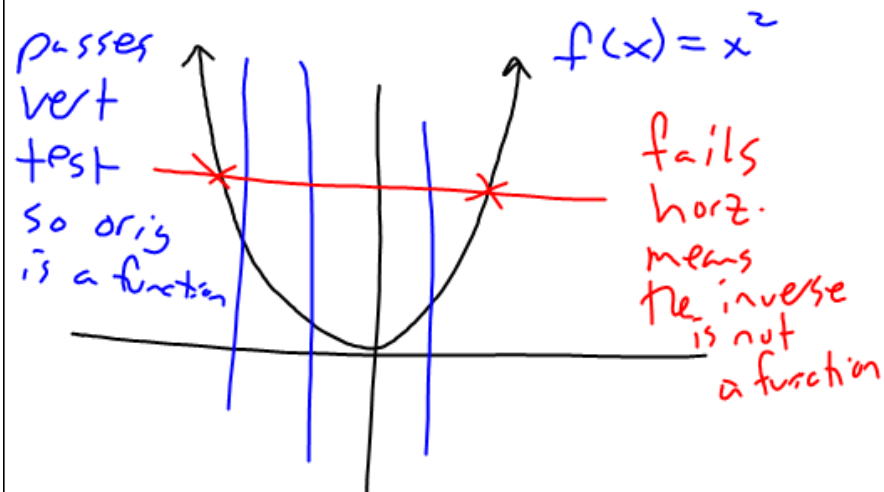
$$f(x) = 3(x+4)^2 - 1$$

$$f(x) = -\frac{1}{2}|x-1| + 2$$

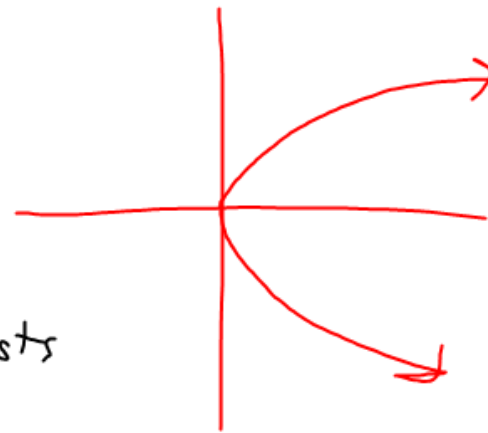


Vertical Line Test - Answers the question - is the original equation a function?

Horizontal Line Test - Answers the question - will the inverse be a function?



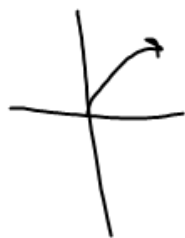
$$f(x) = \pm\sqrt{x}$$



One-to-one functions pass both tests

$$f(x) = \sqrt{x}$$

orig.



$$f(x) = x^2$$

inverse



$$2f(x+3) - 2$$

$$2(x+3)^2 - 2$$

$$2\sqrt{x+3} - 2$$

$$2|x+3| - 2$$

$$2(x+3)^3 - 2$$

$$f(x) = x^2 - x + 1$$

$$f(x+h) = \underline{(x+h)^2} - (x+h) + 1$$

$$\frac{(x+h)(x+h) + x^2 + 2xh + h^2 - x - h + 1 - (x^2 - x + 1)}{h}$$

$$\frac{\cancel{x^2} + 2xh + \cancel{h^2} - \cancel{x} - \cancel{h} + 1 - \cancel{x^2} + \cancel{x} - 1}{h}$$

$$\frac{2xh + h^2 - h}{h}$$

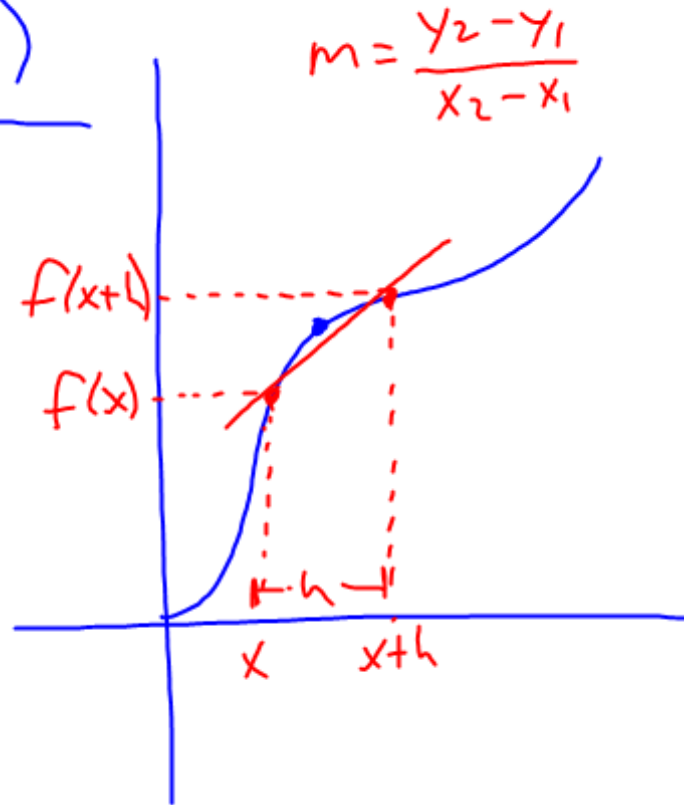
$$\Rightarrow 2x - 1 + h$$

when $x=2$

$$2(2) - 1 + h$$

$$\underline{3 + h}$$

$$\frac{f(x+h) - f(x)}{h}, \quad h \neq 0 \quad \text{D:}$$



5 good Problems

① Find the inverse $f(x) = 3\left(\frac{\sqrt{x-4}}{7}\right)$, is it 1 to 1?

② Graph w/o calc. $f(x) = -3\sqrt{4-x} + 5$

③ Find Difference Quotient (p. 23)

(a) $f(x) = 5x - 7$

(b) $f(x) = 5x^2 - x + 8$

(c) $f(x) = x^3 - 4x$

$$\frac{f(x+h) - f(x)}{h}$$